

OCT 25, 1963

LETTER TO IVOR DARREG AND JOHN CHALMERS FROM ERVIN WILSON

I KNOW ITS A DRAG, BABYS, TO BE BROUGHT DOWN BY PSEUDO-ERUDITE (LIKE,
DOUBLE-WOW, YOU KNOW WHAT I MEAN) RANTINGS ON MANTISSI OF LOGS BASE 2
and all THAT JAZZ---WHEN ALL WE REALLY WANT TO DO IS MAKE WAY OUT SOUNDS.
BUT THERE IS A LITTLE DIRTY WORK TO BE DONE BEFORE WE CAN ALL GET STONED
ON HARMONICS, SO HERE WE GO---LIKE A HERD OF TURTLES, UGH!

Rough Note on Logarithmic Spiral, & Harmonic Series

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Remember that the Octave is the ratio $\frac{2}{1}$, and that the first two terms of the harmonic series are 1 and 2. Consider the circumstance of describing the Harmonic Series logarithmically; For computational clarity one may choose to Take the 8ve as the measuring unit, and describe the series as decimal fractions of the Octave — which as it turns out are logarithms to the base 2 (\log_2). What are logarithms to the base 2? They are the powers to which 2 ($\frac{2}{1}$) must be raised to equal 1, 2, 3, 4, 5, 6, 7, 8, ... the terms of the harmonic series.

Powers of 2 harmonic $\times 360^\circ$ (angular position around circle)

2^0	= 1	$0 \times 360^\circ = 0$
2^1	= 2	$1 \times 360^\circ = 360^\circ (= 1 \text{ octave})$
$2^{1.584962501}$	= 3	$1.585 \times 360^\circ = 360^\circ + .585\dots$
2^2	= 4	$2 \times 360^\circ = \text{twice around circle, to } 0^\circ$
$2^{2.321928095}$	= 5	$2.322 \times 360^\circ = 2 \text{ laps around circle, } +.322$
$2^{2.584962501}$	= 6	$2.585 \times 360^\circ = 2 \text{ laps } + .585$
$2^{2.807354922}$	= 7	$2.807 \times 360^\circ = 2 \text{ laps } + .807$
2^3	= 8	$3 \times 360^\circ = 3 \text{ laps, to } 0^\circ$
$2^{3.169925001}$	= 9	etc
$2^{3.321928095}$	= 10	
$2^{3.459431619}$	= 11	
$2^{3.584962501}$	= 12	
$2^{3.700439718}$	= 13	
$2^{3.807354922}$	= 14	
$2^{3.906890596}$	= 15	
2^4	= 16	

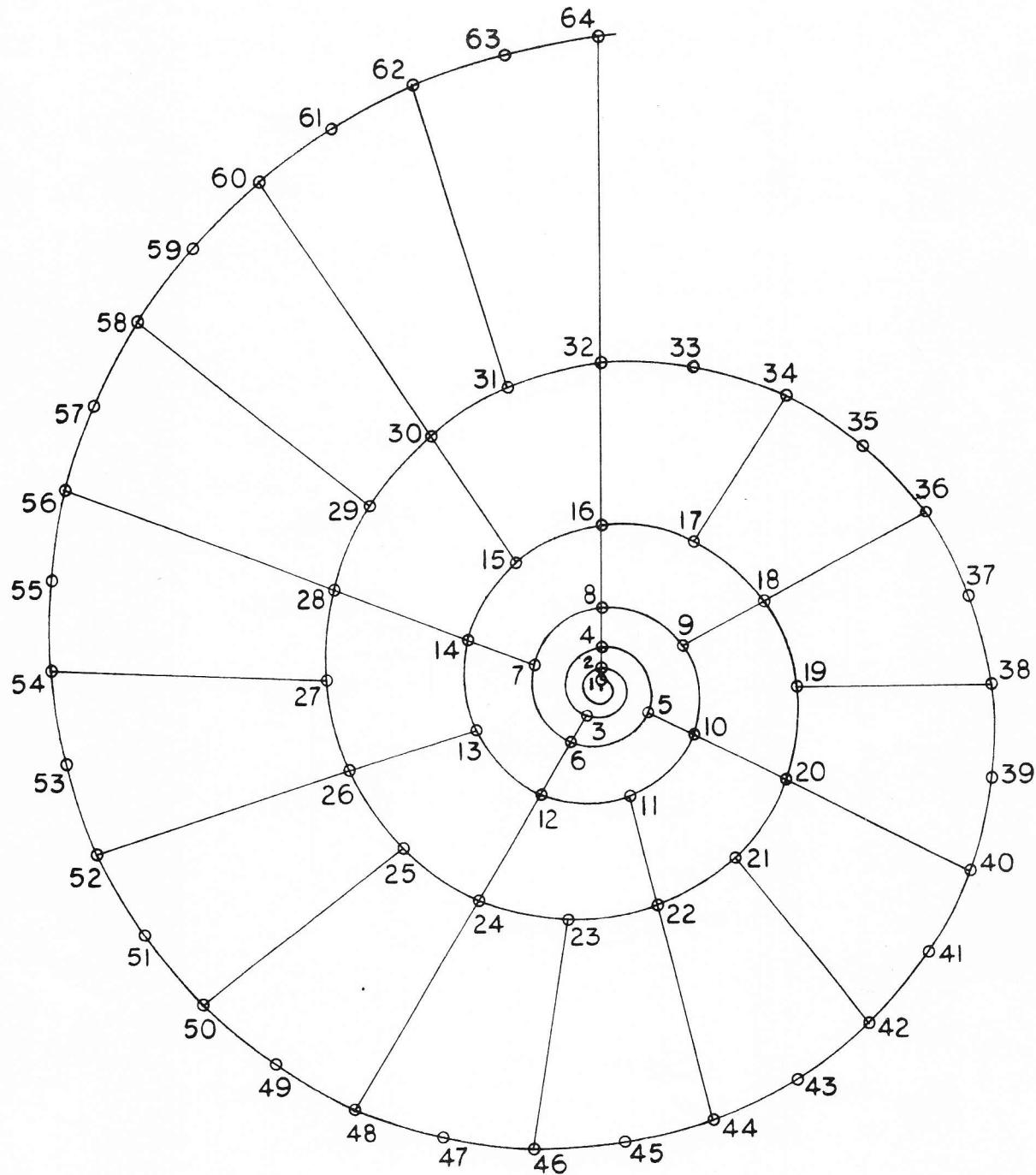
and so forth endlessly

$2^{.694241914} = 1.618033989$ the Golden Section ϕ

I use the hp 20s, hand-held calculator to do these calculations.

THE HARMONIC SERIES AS A LOGRITHMIC SPIRAL

Issued by Erv Wilson March 1, 1965

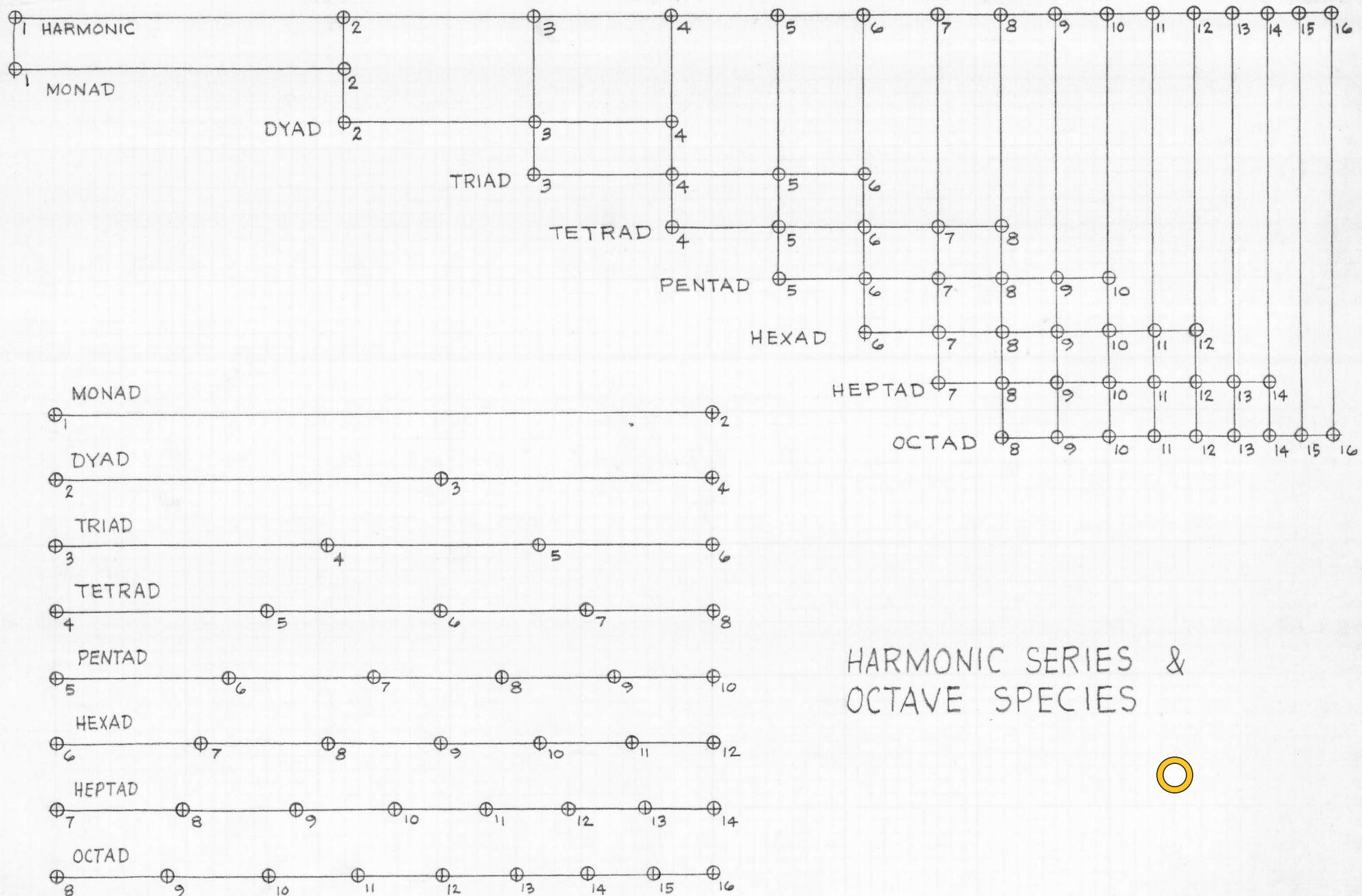


LOGARITHMS TO THE BASE 2 OF THE NUMBERS 1 TO 64

Issued Oct. 21, 1964 by Erv Wilson

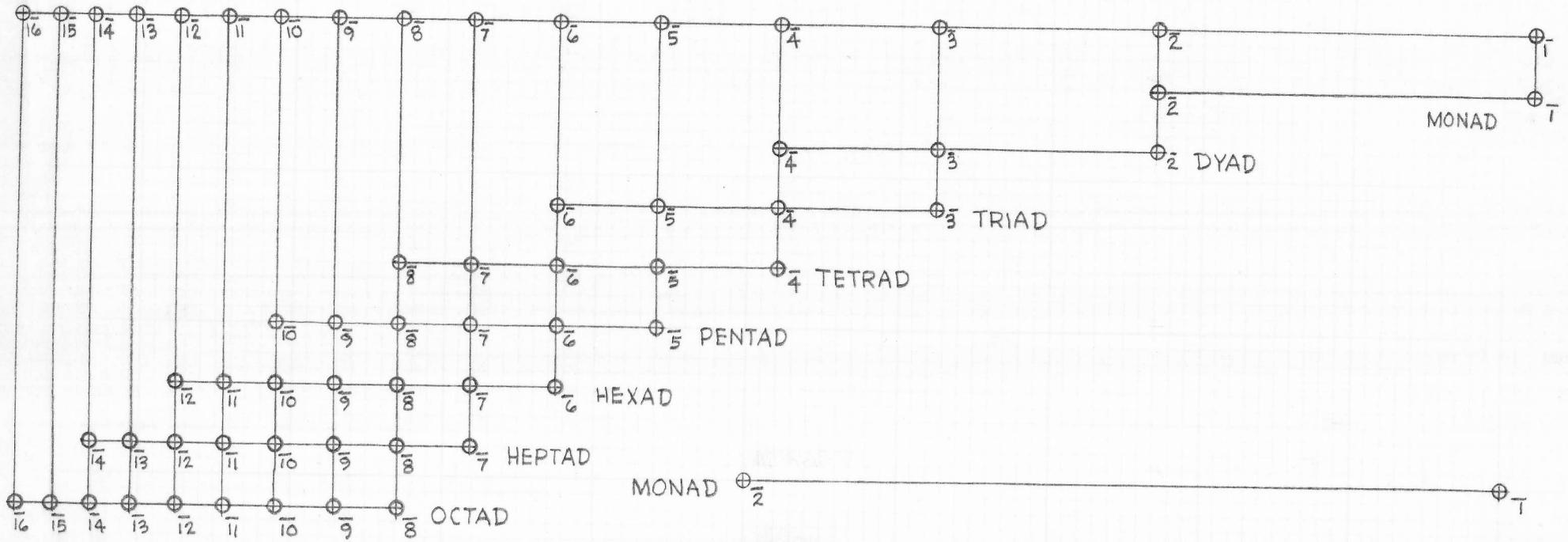
1.	0.0000 0000	33.	5.0443 9412
2.	1.0000 0000	34.	5.0874 6284
3.	1.5849 6250	35.	5.1292 8301
4.	2.0000 0000	36.	5.1699 2500
5.	2.3219 2809	37.	5.2094 5336
6.	2.5849 6250	38.	5.2479 2751
7.	2.8073 5492	39.	5.2854 0221
8.	3.0000 0000	40.	5.3219 2809
9.	3.1699 2500	41.	5.3575 4868
10.	3.3219 2809	42.	5.3923 1742
11.	3.4594 3162	43.	5.4262 6475
12.	3.5849 6250	44.	5.4594 3162
13.	3.7004 3971	45.	5.4918 5309
14.	3.8073 5492	46.	5.5235 6195
15.	3.9068 9059	47.	5.5545 8885
16.	4.0000 0000	48.	5.5849 6250
17.	4.0874 6284	49.	5.6147 0984
18.	4.1699 2500	50.	5.6438 5618
19.	4.2479 2751	51.	5.6724 2534
20.	4.3219 2809	52.	5.7004 3971
21.	4.3923 1742	53.	5.7279 2045
22.	4.4594 3162	54.	5.7548 8750
23.	4.5235 6195	55.	5.7813 5971
24.	4.5849 6250	56.	5.8073 5492
25.	4.6438 5618	57.	5.8328 9001
26.	4.7004 3971	58.	5.8579 4777
27.	4.7548 8750	59.	5.8823 1085
28.	4.8073 5492	60.	5.9068 9059
29.	4.8579 4777	61.	5.9307 3733
30.	4.9068 9059	62.	5.9541 9639
31.	4.9541 9639	63.	5.9772 7992
32.	5.0000 0000	64.	6.0000 0000

I originally calculated these around 1950-1951
at BYU. Erv Wilson



HARMONIC SERIES &
OCTAVE SPECIES





SUBHARMONIC SERIES
& OCTAVE SPECIES

